

Applications | Connections | Extensions



Applications

- 1. Show two ways three people can share a 5-segment chewy fruit worm.
- 2. Show two ways five people can share a 3-segment chewy fruit worm.
- **3.** Sharon is ready to share the 4-segment chewy fruit worm shown below. She has already made the marks she needs so that she can share it equally among the members of her group.

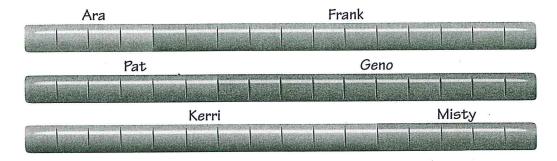


- **a.** Give two different numbers of people that could be in Sharon's group.
- **b.** For each answer you gave in part (a), write a ratio comparing the number of people sharing a chewy fruit worm to the number of segments they are sharing. How would you rewrite this as a unit rate?
- **4.** Cheryl, Rita, and four of their friends go to a movie and share a 48-ounce bag of popcorn equally and three 48-inch licorice laces equally. Write a ratio comparing the number of ounces of popcorn to the number of friends. Then, write a unit rate comparing the length of licorice lace for each person.
- **5.** The Lappans buy three large sandwiches to serve at a picnic. Nine people come to the picnic. Show three different ways to cut the sandwiches so that each person gets an equal share.
- **6.** Three neighbors are sharing a rectangular strip of land for a garden. They divide the land into 24 equal-sized pieces. They each get the same amount of land. Write a ratio comparing the number of pieces of land to the number of people. Write the answer in more than one way.





7. For each chewy fruit worm below write the possible ages of the two people sharing the worm by age.



Use this information for Exercises 8–10. At the birthday party in Problem 2.2, the children run relay races. The distance each team member runs depends on the ratio of their ages. For example, a boy who is twice as old as a girl runs twice as far.

- **8.** Crystal is 12 years old and Alexa is 6 years old. If Crystal runs 100 yards, how far does Alexa run? How far do they run altogether?
- **9.** Jared is 10 years old and Peter is 15 years old. Together, they run 150 yards. How far does each brother run?
- **10.** Wynne and Emmett are brother and sister. Wynne runs 180 yards. Emmett runs 120 yards. How old could each of them be?

Use this information for Exercises 11–14. Parents are older than their children. The ratio of a parent's age to a child's age changes as the parent and child get older.

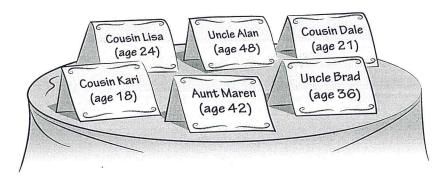
- 11. Can a parent ever be exactly twice as old as his or her child? Explain.
- **12.** Can a parent ever be exactly three times as old as his or her child? Explain.
- **13.** Can the ratio of a parent's age to his or her child's age ever be exactly 3:2? Explain.
- **14.** Can the ratio of a parent's age to his or her child's age ever be exactly 10:9? Explain.



15. Crystal and Alexa convince the older members of their family to break up the chewy fruit worms using age ratios. They want to know which family members have the same age ratio as Crystal and Alexa.



a. Use the ages of their family members to find pairs that have the same age ratio as Crystal (age 12) and Alexa (age 6).



b. What do all the ratios that you wrote in part (a) have in common?

For Exercises 16-18, copy and complete the table comparing the chewy fruit worm segments each family member received. State both unit rates in each comparison.

16. 7 48 12 1 1 8 Segments for Lisa 24

17. 1 33 24 12 $1\frac{1}{2}$ 2 1 6 200

18. 1 Segments for Alan 48 24 $1\frac{1}{2}$ 6 2





For Exercises 19–22, use the family members from Exercise 15, including Crystal and Alexa. Determine which two people have each age ratio.

- **19.** The unit rate is 2:1.
- **20.** The unit rate is 4:1.
- 21. The ratio of segments (ages) is 3:4.
- **22.** The ratio of segments (ages) is 3:2.

For Exercises 23 and 24, Rosco is planning meals for his family. He uses the vertical rate tables.

23. a. Complete the rate table for the macaroni and cheese ingredients.

Macaroni and Cheese

Ounces of Macaroni	Cups of Cheese	
8	1	
1743	2	
E	3	
	4	
	5	
M	6	

- **b.** How many ounces of macaroni would you need for 7 cups of cheese?
- **c.** How many cups of cheese would you need for 88 ounces of macaroni?



Connections

24. a. Complete the rate table for the spaghetti ingredients.

Spaghetti and Sauce

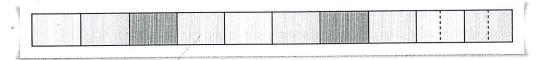
1 5	445-140 0 1000-1400 3-400 3400 3500 5000 5000	
Ounces of	Ounces of Tomatoes	
Spaghetti		
12	16	
6	8	
3		
2		
1		

- **b.** What is the unit rate comparing the number of ounces of tomatoes to 1 ounce of spaghetti?
- c. What is the unit rate comparing 1 ounce of tomatoes to the number of ounces of spaghetti?

Connections

- 25. Ursula, Ubaldo, Ulysses, and Dora were trying to come up with different ways to divide a 10-segment chewy fruit worm among the four of them. Which of these strategies would result in sharing equally?
 - Ursula's Strategy:

Give everyone two segments, and then divide the remaining two segments into four equal pieces with each person getting another half of a segment.



Ubaldo's Strategy:

Give each person one segment, then if there's at least four segments left, give each person another segment. Repeat this process until there are less than four segments, then cut the leftover pieces into four equal parts and give each person a part.

- Ulysses' Strategy:
 - Give each person two segments, and then use a spinner to pick the winner of the extra two segments.
- Dora's Strategy:

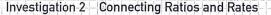
Forget about the segments. Just cut the worm in half, and then cut each half in half again.





- **26.** If you were going to make segment marks on a chewy fruit worm without any marks, what would be the advantage or disadvantage of using a prime number of segments?
- **27.** A typical container of orange juice concentrate holds 12 fluid ounces (fl oz). The standard recipe is "Mix one can of concentrate with three cans of cold water."
 - a. What is the ratio of concentrate to water?
 - **b.** How large of a container will you need to hold the juice?
 - **c.** Olivia has a one-gallon container to fill with orange juice. She uses the standard recipe. How much concentrate does she need? (One gallon is 128 fl oz.)
- **28.** A typical container of lemonade concentrate holds 12 fl oz. The standard recipe is "Mix one can of concentrate with $4\frac{1}{3}$ cans of cold water."
 - a. What is the ratio of concentrate to water?
 - **b.** How large of a container will you need to hold the lemonade?
 - **c.** Olivia has a one-gallon container to fill with lemonade. She uses the standard recipe. How much concentrate does she need? (One gallon is 128 fl oz.)





29. Langhus Convenience Store sells multiple sizes of chewy fruit worms. Betsy, Emily, and John are trying to decide which of the deals would give them the most chewy fruit worms for the price.

Applications





- a. Which argument do you think is the best? Explain.
 - Betsy: The small size is the best deal because you get the most amount of worms, 10 more than the medium size, and 18 more than the large size.
 - John: The large size is the best deal because you have to pay the least amount of money overall.
 - Emily: I used the least common multiple of 4, 8, and 12, which is 24. For \$24, I could buy 60 large worms, 54 medium worms, and 56 small worms. The large size is the best deal.
- **b.** How could Betsy, John, and Emily use unit rates to find the best deal?
- **30.** As Johann is working on unit rates in Exercises 16–24, he notices something interesting and says to his teacher, "Whenever you compare two quantities and you write both unit rates, at least one of them will have a fraction in it." Is Johann correct? Explain why you agree or disagree with him.





Extensions

For Exercises 31–33, consider the conjectures Jena made while working on Problem 2.1. Which conjectures do you think are true? Explain.

- **31.** If the number of people is greater than the number of segments, each person will get less than one segment.
- **32.** There are at least two ways to divide any chewy fruit worm so that everyone will get the same amount.
- **33.** If the ratio of people to segments is 1 : 2, then each person will get $\frac{1}{2}$ of a segment.
- 34. Harold is eight years older than Maynard. On Harold's sixteenth birthday, he notices something interesting about their age ratios. He says, "When I was nine, the ratio of my age to Harold's was 9:1. A year later the ratio was 5:1. That's when I was ten and Maynard was two. Now on my sixteenth birthday, I'm twice as old as Maynard, which means the ratio of our ages is 2:1." Will Harold and Maynard ever have an age ratio 1:1? Explain.
- **35.** A women's 4-by-100 meter medley relay team finished in second place. In the relay, each member swims 100 meters using a different stroke. The ages of the team members are 21, 22, 25, and 41.

The age difference between the oldest and youngest swimmer on this team was 20 years!

Suppose they had broken up the distance of 400 meters by age as in Problem 2.2. How far would each person swim in the relay?

- **36.** Mariette, Melissa, and Michelle were given this follow-up question by Mr. Mirasola to Problem 2.3, "If you had \$3.55, how many large chewy fruit worms could you buy?"
 - Mariette said that she could buy $35\frac{1}{2}$.
 - Melissa said that she could buy only 35.
 - Michelle said that she could buy only 30.
 Mr. Mirasola said, "You are all correct dependent."

Mr. Mirasola said, "You are all correct depending on how you think of the ad." How is it possible that they could all be correct?

Investigation 2



- **37.** On a recent trip to Canada, Tomas learned that there was an "exchange rate" between U.S. dollars and Canadian dollars. When he exchanged his U.S. dollars, he did not get the same number of Canadian dollars back. Tomas hopes to visit many different countries one day, so he does some research and finds a Web site with some basic money conversions on it.

a. Find the unit rate for each country below.

Currency Exchange Rates

\$20 US ~ 19 Australian Dollars	\$1 US ≈ ■ AUD	\$ US ≈ 1 AUD
\$5 US ~ 4 Euros	\$1 US ≈ ■ Euros	\$ US ≈ 1 Euro
\$50 US ≈ 49 Swiss Francs	\$1 US ≈ ■ SF	\$ US ≈ 1 SF
\$3 US ≈ 2 Pounds (UK)	\$1 US ≈ M Pounds	\$ US ≈ 1 Pound
\$4 US ~ 5 Singapore Dollars	\$1 US ≈ ■ SGD	\$ US ≈ 1 SGD

Note: Exchange rates often change from day to day; there are Web sites that have the most up-to-date exchange rates.

b. How can you use this information to convert euros to Australian dollars or Swiss francs to Singapore dollars? Explain.

5000 Japanese yen, Ichiyo Higuchi (1872–1896), writer and poet 10 US dollars, Andrew Jackson (1767–1845), seventh President



10 English pounds, Queen Elizabeth II (b. 1926)

20 Australian dollars, Mary Reibey (1777–1855), businesswoman



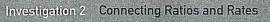
Mathematical Reflections

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In this Investigation, you used ratios to share equally and unequally according to certain rules. You used rate tables and unit rates to solve problems. These questions will help you summarize what you have learned.

Think about your answers to these questions. Discuss your ideas with other students and your teacher. Then write a summary in your notebook.

- 1. a. How can you determine a unit rate for a situation?
 - b. Describe some ways that unit rates are useful.
- 2. a. What strategies do you use to make a rate table?
 - b. Describe some ways that rate tables are useful.
- **3. How** are your strategies for writing equivalent ratios the same as or different from writing equivalent fractions?



Common Core Mathematical Practices

thought about the Problems, and how you used Mathematical Practices. Practices to solve the Problems. Think back over your work, the ways you knowledge to make sense of the Problems. You also applied Mathematical As you worked on the Problems in this Investigation, you used prior

Jayden described his thoughts in the following way:

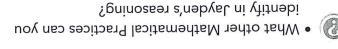
.S.S maldord ni emrow fruit yward to etnuome We used rate tables to find the prices for different

. I & naq amnow a unit rate: the money per each worm or number of to truoms and ni matted eint bassardxa eu to amod ".Od. \$ yeq ot been ew errow & yreve rot" er houe In the rate table, we noticed a repeated pattern

there is a \$ 5 increase for every 50 worms. worms, we used our rate table and noticed that In figuring out how much we need to pay for 500

Common Core Standards for Mathematical Practice

MP7 Look for and make use of structure



Problem in this Investigation. and your classmates used to solve a different Describe a Mathematical Practice that you

